



A Density Functional Theory analysis of the relationships between the Badger index measuring carcinogenicity and the electronic structure of a series of substituted Benz[a]anthracene derivatives, with a suggestion for a modified carcinogenicity index

Juan S. Gómez-Jeria*, Pablo Castro-Latorre

Quantum Pharmacology Unit, Department of Chemistry, Faculty of Sciences, University of Chile. Las Palmeras 3425, Santiago 7800003, Chile

Abstract We carried out a quantum-chemical analysis of the relationships between the electronic structure of several substituted benz[a]anthracene derivatives and Badger's qualitative scale for grading skin and subcutaneous tissue carcinogenic activity. We obtained statistically significant results for the Badger index used for carcinogenicity in the skin but not for the subcutaneous tissue. A new carbon atom was detected as being important in the carcinogenic process. We defined a new carcinogenic index based on the earliest day of death of tumor-bearing mice. The use of this new index provided better results than Badger's. A carbon atom, never detected previously, appeared in the equation relating structure with carcinogenic potency. The results presented here, together the ones of a previous paper, allow to begin to understand why concepts such as K-L regions, bay region and M-region never were fully satisfactory.

Keywords QSAR, cancer, carcinogenesis, KPG model, benz[a]anthracene, Badger, chemical reactivity

Introduction

The search for obtaining *formal* relationships between electronic structure and carcinogenic activity began around 1946[1-53]. Up to year 2015 no research group succeeded in this task. During year 2016, and employing a physically-based method[54] to link the electronic structure of a group of benz[a]anthracene derivatives with Iball's carcinogenic index and Beremblum's carcinogenic grades, we finally obtained the first formal quantitative results[55]. Iball and Beremblum's indices have a numerical scale. On the other hand, there is a third index proposed by Badger for grading the carcinogenic potency. This qualitative or semi-quantitative scale was defined as follows: ++++ signifies very marked carcinogenic activity (CA), +++ signifies CA, ++ signifies moderate CA, + signifies slight CA and 0 denotes an inactive molecule. Badger says that the error of this scale is *at least* one + symbol. This scale has been used until recent times. The problem is that, to employ Badger's scale in a formal QSAR study, we need to associate it with a numerical scale. This problem needs to be addressed and solved because Badger's scale is still the only way in which carcinogenic activity is reported in some papers.

In this paper we present the results of two quantum-chemical analyses of the relationships between the electronic structure of several carcinogenic substituted benz[a]anthracene derivatives and Badger's scale. These results prompted us to propose a modified Badger index that is presented and analyzed here. The studies are presented consecutively for the sake of clarity.



Models, Methods and Calculations

Starting from the statistical-mechanical definition of the equilibrium constant, a strict relationship between the biological activity and a set of local atomic reactivity indices was developed time ago (the KPG model, [54]). Each atom is described at least by the following local atomic reactivity indices: net charge (Q), total atomic electrophilic superdelocalizability (S^E), total atomic nucleophilic superdelocalizability (S^N), Fukui indices of the three highest occupied local MOs[56], Fukui indices of the three lowest vacant local MOs, electrophilic superdelocalizabilities of the three highest occupied local MOs, nucleophilic superdelocalizabilities of the three lowest vacant local MOs, local atomic electronic chemical potential (μ), local atomic hardness (η), local atomic softness (s), the maximal amount of charge that an atom may receive (Q^{\max}) and local atomic electrophilicity (ω). When needed, the orientational parameters (OP) of the substituents were added to this set [57-59]. We refer the reader to the numerous papers published on the model [60-64], specially to Ref. [54] in which a full detailed description of the method is presented. The hypothesis that the model developed only for receptor affinity constants can be applied to any biological activity has been tested in several different molecular systems and biological activities with complete success ([65-81]and references therein). In one case, my collaborators and I were able to predict the hallucinogenic properties of a molecule and in another case we were able to show that the experimental data was erroneous [82, 83]. Therefore we shall discuss here only the resulting equations. All molecular geometries were fully optimized within the Density Functional Theory with the mPW1PW91 functional and a LanL2DZ basis set. The Gaussian suite of programs was employed [84]. All linear multiple regression analyses (LMRA) were performed using as dependent variable the carcinogenic potency and as independent variables all the local atomic reactivity indices of the atoms composing a common skeleton plus the orientational parameters when needed. The Statistica software was employed [85]. The values of the orientational parameters were taken from the literature [57, 58] or calculated with the Steric software written in our Unit [59]

Part A. Studies with the original Badger index.

A1. Molecules selected for the original set of Badger values.

The transformation of Badger's scale into a numerical one was made as follows. First, we cannot associate + with the number 1 because Badger suggested that the error of his scale could be at least one +. As we work with logarithms this is not a safe approach. Moreover, we found in more recent literature that the symbol 0/+ was introduced for carcinogenic activity. These two facts led us to employ the following rules for avoiding problems in future studies: to the symbol + we assigned the value 3, to the symbol ++ the value 4 and so on. We inspect the literature to create a set of molecules with the Badger index. The final set is shown in Fig. 1 and Table 1. Table 1 also shows the value of the Badger index for skin and subcutaneous tissue. These values were taken from several Tables of Ref. [86].

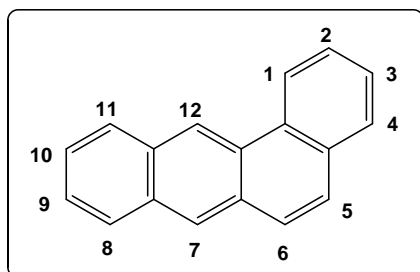


Figure 1: Substituted benz[a]anthracene derivatives

Table 1: Substituted benz[a]anthracene derivatives and carcinogenic activity.

Mol.	Name	Badger (B) Skin	log(B) Skin	Badger (B') Subcutaneous	log(B') Subcut.
1	5-methyl-BA	+	0.48	++	0.60
2	6-methyl-BA	+	0.48	++	0.60
3	7-methyl-BA	+++	0.70	++++	0.78
4	8-methyl-BA	++	0.60	++	0.60
5	9-methyl-BA	+	0.48	nd	--



6	10-methyl-BA	+	0.48	+	0.48
7	11-methyl-BA	+	0.48	nd	--
8	12-methyl-BA	++	0.60	+++	0.70
9	6,7-dimethyl	nd	--	++	0.60
10	6,12-dimethyl-BA	nd	--	+++	0.70
11	7,8-dimethyl-BA	nd	--	++++	0.78
12	7,11-dimethyl-BA	nd	--	+++	0.70
13	7,12-dimethyl-BA	nd	--	+++	0.70
14	8,9-dimethyl-BA	+++	0.70	nd	--
15	8,12-dimethyl-BA	nd	--	++++	0.78
16	9,10-dimethyl-BA	+	0.48	nd	--
17	7,8,12-trimethyl-BA	++++	0.78	+++	0.70
18	7,9,12-trimethyl-BA	++++	0.78	++	0.60
19	7,8,9,12-tetramethyl-BA	+++	0.70	+	0.48
20	8-ethyl-BA	++	0.60	nd	--
21	8-n-propyl-BA	++	0.60	nd	--
22	8-iso-propyl-BA	++	0.60	+	0.48
23	8-n-butyl-BA	++	0.60	nd	--
24	8-n-amyl-BA	++	0.60	nd	--
25	8-n-hexyl-BA	+	0.48	nd	--
26	8-n-heptyl-BA	+	0.48	nd	--
27	7-ethyl-BA	nd	--	+++	0.70
28	7-CH ₂ CN-BA	nd	--	+	0.48
29	7-CH ₂ OH-BA	++	0.60	+++	0.70
30	7-CH ₂ OCOCH ₃ -BA	++	0.60	+++	0.70
31	7-CH ₂ OCH ₂ CH ₃ -BA	+	0.48	nd	--
32	7-CH ₂ COOCH ₃ -BA	nd	--	+	0.48
33	7-OCH ₃ -BA	nd	--	++	0.60
34	7-NH ₂ -BA	nd	--	+	0.48
35	7-CN-BA	+	0.48	++	0.60
36	7-NCO-BA	nd	--	+	0.48
37	7-CHO-BA	nd	--	++	0.60

A2. Results for the original Badger index.

The atoms composing the common skeleton used in this part of the study are shown in Fig. 2. For LMRA we employed all the local atomic reactivity indices of these atoms plus the orientational parameters of the substituents attached to some of them (R_5 to R_{12} of Table 1).

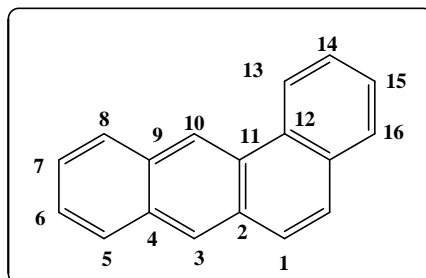


Figure 2: Common skeleton numbering

A.2.1. Results for the skin carcinogenic activity.

The best equation obtained is:

$$\log(B) = 0.56 - 0.65S_2^E(\text{HOMO} - 2)^* + 0.11S_3^E(\text{HOMO} - 2)^* + 0.27S_3^E - 0.00005\varphi_{R8} + 0.34S_{10}^N(\text{LUMO})^* \quad (1)$$



with $n=24$, $R=0.95$, $R^2=0.90$, adjusted $R^2=0.88$, $F(5,18)=34.224$ ($p<0.000001$) and a standard error of estimate of 0.03. Here, $S_2^E(\text{HOMO-2})^*$ is the electrophilic superdelocalizability of the third highest occupied MO localized on atom 2, $S_3^2(\text{HOMO-2})^*$ is the electrophilic superdelocalizability of the third highest occupied MO localized on atom 3, S_3^E is the total atomic electrophilic superdelocalizability of atom 3, φ_{R8} is the orientational parameter of the substituent attached to atom 5 in Fig. 2 (atom 8 in Fig. 1) and $S_{10}^N(\text{LUMO})^*$ is the nucleophilic superdelocalizability of the lowest empty MO localized on atom 10. All atom numbering refers to Fig. 2. Tables 2 and 3 show the beta coefficients, the results of the t-test for significance of coefficients and the matrix of squared correlation coefficients for the variables of Eq. 1. There are no significant internal correlations between independent variables (Table 3). Figure 3 displays the plot of observed vs. calculated values.

Table 3: Beta coefficients and t-test for significance of coefficients in Eq. 1.

Variable	Beta	t(18)	p-level
$S_2^E(\text{HOMO-2})^*$	-0.64	-7.62	<0.000001
$S_3^2(\text{HOMO-2})^*$	0.76	8.09	<0.000001
S_3^E	0.35	4.23	<0.0005
φ_{R8}	-0.37	-4.24	<0.0005
$S_{10}^N(\text{LUMO})^*$	0.23	2.74	<0.01

Table 4: Matrix of squared correlation coefficients for the variables in Eq. 1.

	$S_2^E(\text{HOMO-2})^*$	$S_3^2(\text{HOMO-2})^*$	S_3^E	φ_{R8}
$S_3^2(\text{HOMO-2})^*$	0.13	1.00		
S_3^E	0.16	0.03	1.00	
φ_{R8}	0.07	0.30	0.01	1.00
$S_{10}^N(\text{LUMO})^*$	0.04	0.18	0.08	0.12

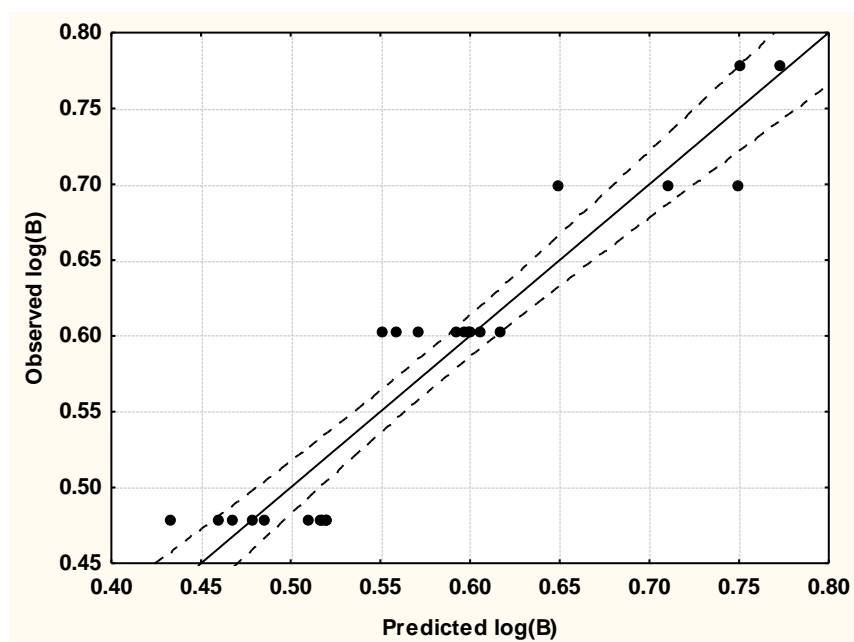


Figure 3: Plot of predicted vs. observed carcinogenic potency (skin, Eq. 1). Dashed lines denote the 95% confidence interval.



The associated statistical parameters of Eq. 1 indicate that this equation is statistically significant and that the variation of the numerical values of a group of five local atomic reactivity indices of atoms of the common skeleton plus one orientational effect of the substituent explains about 88% of the variation of the carcinogenic potency. Figure 3 shows that there is a good correlation of observed *versus* calculated values. Most points are inside the 95% confidence interval but also there are some points located quite far from it.

A.2.2. Results for the subcutaneous carcinogenic activity.

We applied all techniques we used in our previous studies but no statistically significant relationship could be obtained. Only for the effects of providing information we show in Fig. 4 the plot of predicted vs. observed carcinogenic potency for the best equation.

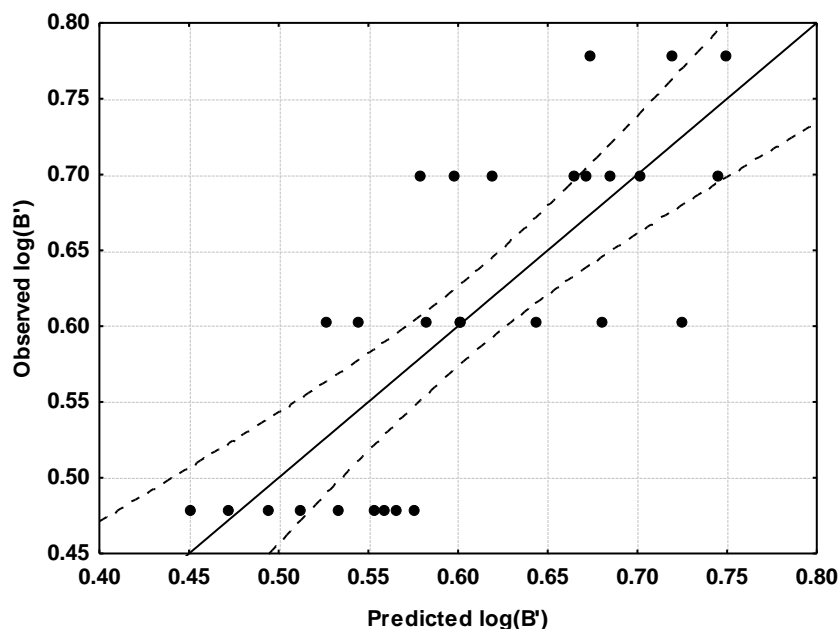


Figure 4: Plot of predicted vs. observed carcinogenic potency (subcutaneous tissue). Dashed lines denote the 95% confidence interval

We can see that the best equation obtained produced very bad results.

A.3. Local Molecular Orbitals.

Table 5 shows the local MO structure of atoms 2, 3 and 10 (see Fig. 2). Nomenclature: Molecule (HOMO) / (HOMO-2)* (HOMO-1)* (HOMO)* - (LUMO)* (LUMO+1)* (LUMO+2)*.

Table 5: Local Molecular Orbitals of atoms 2, 3 and 10 (Eq. 1).

Molecule	Atom 2	Atom 3	Atom 10
1(64)	62π63π64π-65π66π67π	59π60π64π-65π69π70π	62π63π64π-65π66π67π
2(64)	62π63π64π-65π66π67π	60π62π64π-65π69π71π	62π63π64π-65π66π67π
3(64)	62π63π64π-65π66π67π	58σ60π64π-65π69π71π	62π63π64π-65π66π67π
4(64)	62π63π64π-65π66π67π	58σ60π64π-65π67π69π	61π63π64π-65π66π67π
5(64)	62π63π64π-65π66π67π	59π60π64π-65π69π71π	62π63π64π-65π66π67π
6(64)	62π63π64π-65π66π67π	59π60π64π-65π68π69π	62π63π64π-65π66π67π
7(64)	62π63π64π-65π66π67π	59π60π64π-65π67π69π	61π63π64π-65π66π67π
8(64)	62π63π64π-65π66π67π	59π60π64π-65π69π70π	62π63π64π-65π66π67π
9(68)	66π67π68π-69π70π71π	64π66π68π-69π73π75π	66π67π68π-69π70π71π
10(68)	66π67π68π-69π70π71π	64π66π68π-69π73π74π	66π67π68π-69π70π72π
11(68)	66π67π68π-69π70π71π	62σ64π68π-69π73π75π	65π67π68π-69π70π71π
12(68)	66π67π68π-69π70π71π	64π65π68π-69π71π73π	65π67π68π-69π70π71π
13(68)	66π67π68π-69π70π71π	63π64π68π-69π73π75π	66π67π68π-69π70π72π



14(68)	66π67π68π-69π70π71π	62σ64π68π-69π71π73π	65π67π68π-69π70π71π
15(68)	66π67π68π-69π70π71π	63π64π68π-69π71π73π	65π67π68π-69π70π71π
16(68)	66π67π68π-69π70π71π	63π64π68π-69π73π74π	66π67π68π-69π70π71π
17(72)	70π71π72π-73π74π75π	68π69π72π-73π77π79π	69π71π72π-73π74π75π
18(72)	70π71π72π-73π74π75π	67π68π72π-73π77π79π	70π71π72π-73π74π75π
19(76)	74π75π76π-77π78π79π	72π73π76π-77π81π83π	73π75π76π-77π78π79π
20(68)	66π67π68π-69π70π71π	62σ64π68π-69π71π73π	65π67π68π-69π70π71π
21(72)	70π71π72π-73π74π75π	66σ68π72π-73π75π77π	69π71π72π-73π74π75π
22(72)	70π71π72π-73π74π75π	66σ68π72π-73π75π77π	69π71π72π-73π74π75π
23(76)	74π75π76π-77π78π79π	70π72π76π-77π79π81π	73π75π76π-77π78π79π
24(80)	78π79π80π-81π82π83π	74σ76π80π-81π83π85π	77π79π80π-81π82π83π
25(84)	82π83π84π-85π86π87π	79σ80π84π-85π87π89π	81π83π84π-85π86π87π
26(88)	86π87π88π-89π90π91π	83σ84π88π-89π91π93π	85π87π88π-89π90π91π
27(68)	66π67π68π-69π70π71π	62σ64π68π-69π73π75π	66π67π68π-69π70π71π
28(70)	68π69π70π-71π72π73π	64σ66π70π-71π75π77π	68π69π70π-71π72π73π
29(68)	66π67π68π-69π70π71π	65σ66π68π-69π72π73π	66π67π68π-69π70π71π
30(79)	77π78π79π-80π81π82π	74π75π79π-80π83π85π	76π78π79π-80π81π82π
31(76)	74π75π76π-77π78π79π	70σ71π76π-77π79π81π	73π75π76π-77π78π79π
32(75)	73π74π75π-76π77π78π	71σ73π75π-76π78π81π	73π74π75π-76π77π80π
33(68)	66π67π68π-69π70π71π	63π64σ68π-69π73π76π	66π67π68π-69π70π71π
34(64)	62π63π64π-65π66π67π	57σ58π64π-65π69π70π	60π63π64π-65π66π67π
35(66)	64π65π66π-67π68π69π	60σ62π66π-67π70π71π	64π65π66π-67π68π69π
36(70)	68π69π70π-71π72π73π	66π67π70π-71π74π75π	68π69π70π-71π72π73π
37(67)	65σ66π67π-68π69π70π	64π65σ67π-68π73π74π	64π66π67π-68π69π71π

A.4. Discussion of Part A Results.

The first fact to comment on is the origin of the experimental results Badger used to build his Tables used in Part A [86]. An extensive search and full analysis of Badger's papers and the data he employed did not allow us to deduce the logics he used to build his scale. For the very bad results obtained for the carcinogenic potency in subcutaneous tissues, we have three provisional explanations. The first one is that Badger's original scale is wrong in some case. Another possibility is that our change from a qualitative scale to a quantitative one was not correct. This option could be ruled out based on our results on skin. The third one is related to the fact that in subcutaneous tissue the action mechanism of the molecules is not the same. We think that the first explanation is the most probable one.

Regarding the results on skin, Eq. 1 and Table 3 show that the importance of variables is $S_3^E(\text{HOMO-2})^* > S_2^E(\text{HOMO-2})^* > \varphi_{R8} > S_3^E > S_{10}^N(\text{LUMO})^*$. The examination of the coefficients of the variables of Eq. 1 and knowing that a higher Badger index corresponds to a higher carcinogenic activity, allow to suggest that a high activity is associated with high (negative) values of $S_2^E(\text{HOMO-2})^*$, small (negative) values of $S_3^E(\text{HOMO-2})^*$ and S_3^E , small values for φ_{R8} (position 5 in Fig. 2) and high (positive) values for $S_{10}^N(\text{LUMO})^*$. Atom 2 is a carbon without hydrogen atoms bonded to it. Table 5 shows that the three highest occupied local MOs and the three lowest empty local MOs have a π nature. These six local MOs coincide with the molecular MOs. The fact that a high carcinogenic activity is associated with high (negative) values of $S_2^E(\text{HOMO-2})^*$ strongly suggests that this atom is interacting with its first three occupied local MOs with an electron-deficient site. This is important because it is the second time that an unsaturated carbon atom, not found in any other previous study, is detected as participating in the carcinogenic activity. Last year and in this Unit, a structure-carcinogenic activity (sarcoma induction) analysis of several substituted benz[a]anthracene derivatives showed that atom 11 of Fig. 2 seems to be involved in the process [55]. Note that in that study quantitative scales to measure carcinogenic potency were employed. Atom 3 is a carbon atom (Fig. 2, see atom 7 in Fig. 1). A high carcinogenic activity is associated with small (negative) values of S_3^E and $S_3^E(\text{HOMO-2})^*$ (both indices are not correlated, Table 4). Table 5 shows that $(\text{HOMO-2})_3^*$ and $(\text{HOMO-1})_3^*$ are of π or σ in some molecules, while $(\text{HOMO})_3^E$ has a π nature in all molecules. Considering that the best way to obtain small negative values for these indices is by making more negative the MO energies, we suggest that this atom is interacting with a rich-electron center and acting probably as an electron acceptor. Atom 10 is a carbon atom (Fig. 2,



see atom 12 in Fig. 1). Table 5 shows that the three highest occupied local MOs and the three lowest empty local MOs have a π nature, and that they coincide with the molecule's MOs. A high carcinogenic activity is associated with high (positive) values for $S_{10}^N(\text{LUMO})^*$. As these values are obtained by lowering the MO energy and making it more reactive, we suggest that this atom is interacting with an electron-rich center and acting probably as an electron acceptor. Small values for ϕ_{R8} (position 5 in Fig. 2) are associated with high carcinogenic activity. This suggests that hydrogen or methyl substituents are suitable. All the suggestions are displayed in the partial 2D pharmacophore of Fig. 5.

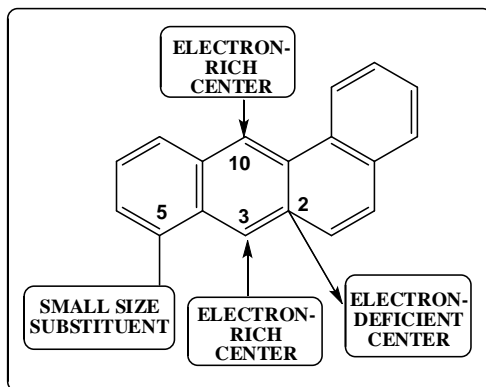


Figure 5: Partial 2D pharmacophore for carcinogenic potency

Part B. Studies with a new carcinogenicity index.

B1. The new index.

The unsatisfactory results obtained for the relationship between subcutaneous carcinogenic activity and electronic structure with the Badger scale pushed us into the task of creating a modified scale. Our goal is twofold. The first one is to analyze the quality of the results obtained using a modified scale built on logical and known foundations. The second one could be perfectly called “the big prize”, which consists in carrying out the study of the activity of many molecules with very different number of aromatic rings. We proceeded as follows. *We hypothesized that the carcinogenic activity is well represented by the earliest day of death of tumor-bearing mice (D)*. Using this data we defined the following rules:

0-100 D = +++++

101-150 D = ++++

151-200 D = +++

201-250 D = ++

251-299 D = +

D larger than 300 = 0/-

Next, we made the following associations: +++++=7, ++++=6, +++=5, ++=4, +=3, 0/-=2. Our scale is quite similar to Beremblum's one, but he used the latency period in weeks or the time of appearance of the first tumor.

B2. Molecules selected for part B.

We selected a small group of substituted benz[a]anthracene derivatives showing carcinogenic activity on the skin of mice (papilloma and epithelioma) [87, 88]. The molecules are displayed in Figure 6 and Table 6.



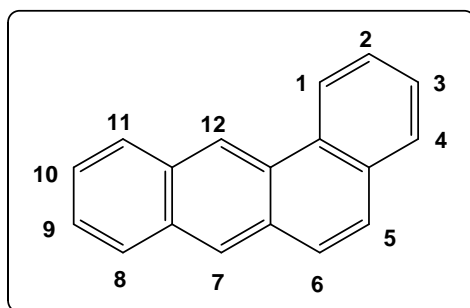


Figure 6: Selected molecules

Table 6: Substituted benz[a]anthracene derivatives and the new index (E).

Mol.	Name	A	E	log(E)
1	5-methyl	0/-	2	0.30
2	7-methyl	++++	6	0.78
3	10-methyl	0/-	2	0.30
4	11-methyl	0/-	2	0.30
5	12-methyl	+	3	0.48
6	7,12-dimethyl	+++++	7	0.85
7	7,9,12-trimethyl	++++	6	0.78
8	7,8,9,12-tetramethyl	+++++	7	0.85
9	8-iso-propyl	0/-	2	0.30
10	8-n-butyl	0/-	2	0.30
11	8-n-amyl	++	4	0.60
12	8-n-hexyl	0/-	2	0.30
13	8-n-heptyl	0/-	2	0.30
14	7-CH ₂ OH	++	4	0.60
15	7-CH ₂ OCOCH ₃	++	4	0.60
16	7-CN	0/-	2	0.30

B3. Results for the new index.

The common skeleton numbering is shown in the following figure.

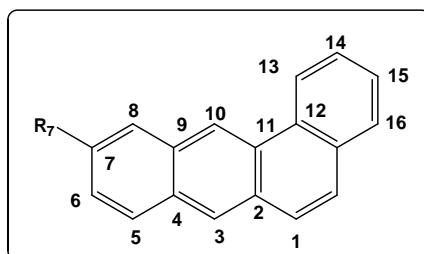


Figure 7: Common skeleton numbering

The best equation obtained is the following:

$$\log(E) = -7.18 - 0.96S_2^E + 0.72S_9^N(\text{LUMO})^* - 0.003\varphi_7 \quad (2)$$

with $n = 15$, $R = 0.99$, $R^2 = 0.98$, adjusted $R^2 = 0.97$, $F(3,11) = 164.51$ ($p < 0.000001$) and a standard error of estimate of 0.04. Here, S_2^E is the electrophilic superdelocalizability of atom 2, $S_9^N(\text{LUMO})^*$ is the nucleophilic superdelocalizability of the highest local MO localized on atom 9 and φ_7 is the orientational parameter of the R_7 substituent. All atom numbering refers to Fig. 7. Tables 7 and 8 show the beta coefficients, the results of the t-test for significance of coefficients and the matrix of squared correlation coefficients for the variables of Eq. 2. There are no



significant internal correlations between independent variables (Table 4). Figure 8 displays the plot of observed vs. calculated values.

Table 7: Beta coefficients and t-test for significance of coefficients in Eq. 2.

Variable	Beta	t(11)	p-level
S_2^E	-1.07	-21.37	0.000001
$S_9^N(\text{LUMO})^*$	0.33	6.49	0.00005
φ_7	-0.15	-2.99	0.01

Table 8: Matrix of squared correlation coefficients for the variables in Eq. 2.

	S_2^E	$S_9^N(\text{LUMO})^*$	φ_7
S_2^E	1		
$S_9^N(\text{LUMO})^*$	0.19	1	
φ_7	0.03	0.07	1

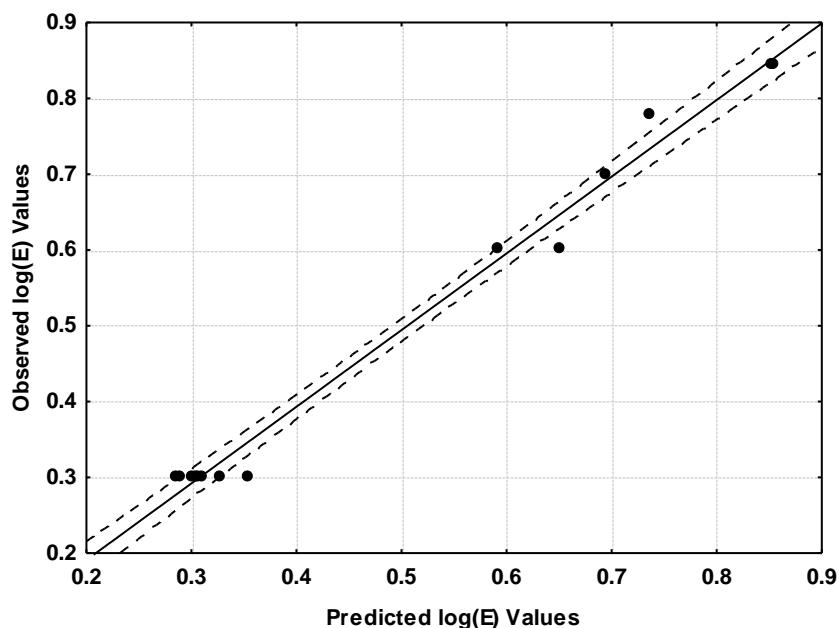


Figure 8: Plot of predicted vs. observed carcinogenic potency (Eq. 2). Dashed lines denote the 95% confidence interval

The associated statistical parameters of Eq. 2 indicate that this equation is statistically significant and that the variation of the numerical values of a group of three local atomic reactivity indices of atoms of the common skeleton explains about 97% of the variation of the carcinogenic activity. Figure 8, spanning about 0.5 orders of magnitude, shows that there is a good correlation of observed *versus* calculated values and that almost all points are inside the 95% confidence interval.

B.4. Discussion of Part B results.

Table 3 shows that the importance of variables is $S_2^E \gg S_9^N(\text{LUMO})^* > \varphi_7$. The examination of the coefficients of the variables of Eq. 2 and knowing that a higher modified index corresponds to a higher carcinogenic activity, allow to suggest that a high activity is associated with high (negative) values for S_2^E , high positive values for $S_9^N(\text{LUMO})^*$ and small values for the orientational parameter of the R_7 substituent. High negative values for S_2^E are associated



with high carcinogenic activity. Higher negative values are obtained by shifting upwards the energies of the occupied MOs. As the local HOMO is the dominant term in the electrophilic superdelocalizability definition (if there is HOMO degeneracy the contribution is greater), we require then a more reactive MO. This suggests that atom 2 is interacting with an electron-deficient center, probably donating electrons to it. Interestingly, in part A of this study (see above and also Ref. [55]) the same atom appears to be significant in the corresponding equation. As this is the third time that this atom appears, we hold that this fact proves its importance in the carcinogenic activity. High positive values for $S_9^N(\text{LUMO})^*$ are associated with high carcinogenic activity (Fig. 7). This MO has a π nature in all molecules. High positive values are obtained by shifting downwards the energy of $(\text{LUMO})_9^*$. As this makes this MO more reactive, we suggest that atom 9 is interacting with an electron-rich center through at least its first empty local MO. Atom 9 has not hydrogen atoms bonded to it, and this is the first time that it appears to be significant. No previous QSAR study pointed to it. Small values of the orientational parameter of the R_7 substituent (φ_7) are associated with high activity. Therefore, a hydrogen atom is preferred over a methyl group. All the suggestions are displayed in the partial 2D pharmacophore of Fig. 9.

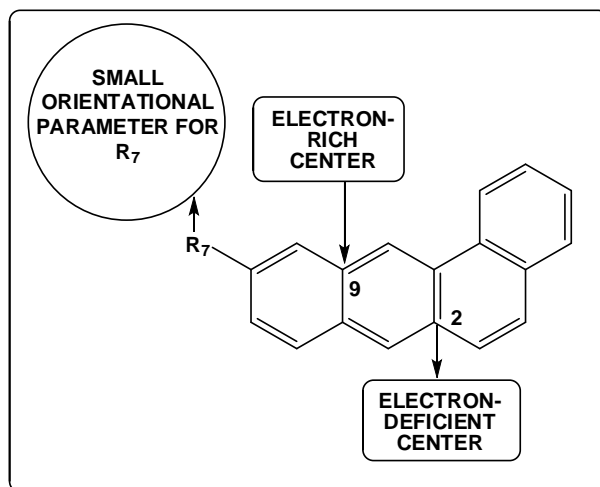


Figure 9: Partial 2D pharmacophore for carcinogenic potency

The previous result and the ones presented here point to the fact that the carcinogenic activity is not only regulated by the carbon atoms with a hydrogen atom or other substituents attached to them, but also by carbon atoms without substituents. This fact can be explained by suggesting that these compounds are placing themselves in such a way that many carbon atoms, with or without hydrogen atoms bond to them, interact simultaneously with the site through their π electron system. *If this suggestion is true, then suggestions such as K-L regions, bay region and M-region are notoriously incomplete.*

Conclusions

In conclusion, we have obtained relevant relationships between the carcinogenic potency and the electronic structure of some benz[a]anthracene derivatives. New carbon atoms that seem to participate in the carcinogenic activity were detected that were not considered in K-L regions, bay region and M-region models.

References

1. Daudel, R. Les théories physicochimiques du cancer. *Revue Scientifique* **1946**, 84, 37-42.
2. Pullman, A. Une méthode de calcul de l'influence des substituants sur la répartition des charges électroniques d'une molécule aromatique. Application à certains carbures cancérigènes. *Comptes Rendus de l'Académie des Sciences* **1946**, 222, 392-394.
3. Pullman, A.; Pullman, B. Structure électronique et pouvoir cancérigène des molécules organiques. *Revue Scientifique* **1946**, 84, 145-158.



4. Pullman, A.; Pullman, B. Répartition du nuage électronique et réactivité chimique des hydrocarbures aromatiques condensés. *Experientia* **1946**, 2, 364-367.
5. N., B.-H.; Daudel, P.; Daudel, R.; Lacassagne, A.; Lecocq, J.; Martin, M.; Rudali, G. Sur une tentative de prévision du pouvoir cancérigène des substances chimiques. *Comptes Rendus de l'Académie des Sciences (Paris)* **1947**, 225, 238-240.
6. Pullman, A. Influence de l'addition des cycles saturés sur la structure électronique et sur l'activité cancérigène des hydrocarbures polycycliques. *Comptes Rendus de l'Académie des Sciences (Paris)* **1947**, 224, 120-122.
7. Pullman, B. Sur la structure électronique des phénylethylènes et le pouvoir cancérigène des azoïques. *Comptes Rendus de l'Académie des Sciences (Paris)* **1947**, 224, 1773-1774.
8. Kooyman, E.C.; Heringa, J.W. Extension of the K-Region Hypothesis of Carcinogenic Chemical Compounds. *Nature* **1952**, 170, 661-662.
9. Coulson, C.A. Electronic Configuration and Carcinogenesis. In *Advances in Cancer Research*, Jesse, P. G.; Alexander, H., Eds. Academic Press: 1953; Vol. Volume 1, pp 1-56.
10. Pagés-Flon, M.; Buu-Hoï, N.P.; Daudel, R. Étude d'une relation entre pK et pouvoir cancérigène pour deux séries de benzacridines. *Comptes Rendus de l'Académie des Sciences (Paris)* **1953**, 236, 2182-2184.
11. Badger, G.M. Chemical Constitution and Carcinogenic Activity. *Advances in Cancer Research* **1954**, 2, 73-127.
12. Nagata, C.; Fukui, K.; Yonezawa, T.; Tagashira, Y. Electronic Structure and Carcinogenic Activity of Aromatic Compounds: I. Condensed Aromatic Hydrocarbons. *Cancer Research* **1955**, 15, 233-239.
13. Pullman, A.; Pullman, B. Electronic Structure and Carcinogenic Activity of Aromatic Molecules New Developments. In *Advances in Cancer Research*, Jesse, P. G.; Alexander, H., Eds. Academic Press: 1955; Vol. Volume 3, pp 117-169.
14. Pullman, A.; Pullman, B. *Cancérisation par les substances chimiques et structure moléculaire*. Masson: Paris, 1955.
15. Badger, G.M. Miscellaneous Chemical Carcinogens: Chemical Constitution and Carcinogenic Activity. *British Journal of Cancer* **1956**, 10, 330-356.
16. Lacassagne, A.; Buu-Hoï, N.P.; Daudel, R.; Zajdela, F. The Relation between Carcinogenic Activity and the Physical and Chemical Properties of Angular Benzacridines. In *Advances in Cancer Research*, Jesse, P. G.; Alexander, H., Eds. Academic Press: 1956; Vol. Volume 4, pp 315-369.
17. Fernández-Alonso, J.I.; Vila, L.C.; Domingo, R. Theoretical Study of Nitrogen Heterocyclics. II. Molecular Diagrams and Carcinogenic Activities of Some Mono- and Dibenzocarbazoles. *Journal of the American Chemical Society* **1957**, 79, 5839-5844.
18. Lacassagne, A.; Buu-Hoï, N.P.; Zajdela, F. Relation entre structure moléculaire et activité cancérigène dans trois séries d'hydrocarbures aromatiques hexacycliques. *Comptes Rendus de l'Académie des Sciences (Paris)* **1958**, 1477-1480.
19. Szent-Györgyi, A.; Isenberg, I.; Baird, S.L. On the Electron Donating properties of carcinogens. *Proceedings of the National Academy of Sciences* **1960**, 46, 1444-1449.
20. Koutecky, J.; Zahradnik, R.; Cizek, J. Relationship between quantum-chemical indices of reactivity of polycyclic alternant hydrocarbons. *Transactions of the Faraday Society* **1961**, 57, 169-182.
21. Arcos, J.C.; Arcos, M. Molecular Geometry and Mechanisms of Action of Chemical Carcinogens. In *Fortschritte der Arzneimittelforschung / Progress in Drug Research / Progrès des recherches pharmaceutiques*, Jucker, E., Ed. Birkhäuser Basel: Basel, 1962; pp 407-581.
22. Allison, A.C.; Nash, T. Electron Donation and Acceptance by Carcinogenic Compounds. *Nature* **1963**, 197, 758-763.



23. Lacassagne, A.; Buu-Hoi, N.P.; Zajdela, F.; Jacquignon, P.; Périn, F. Relations entre structure moléculaire et activité cancérigène chez les benzopyridocarbazoles et les composés polycycliques analogues. *Comptes Rendus de l'Académie des Sciences (Paris)* **1963**, 257, 818-822.
24. Pullman, B.; Pullman, A. Electron-Donor or Electron-Acceptor Properties and Carcinogenic Activity of Organic Molecules. *Nature* **1963**, 199, 467-469.
25. Huggins, C.B.; Pataki, J.; Harvey, R.G. Geometry of carcinogenic polycyclic aromatic hydrocarbons. *Proceedings of the National Academy of Sciences* **1967**, 58, 2253-2260.
26. Mainster, M.A.; Memory, J.D. Superdelocalizability indices and the Pullman theory of chemical carcinogenesis. *Biochimica et Biophysica Acta (BBA) - General Subjects* **1967**, 148, 605-608.
27. Bergmann, E.D.; Pullman, B. *Physico-chemical mechanisms of carcinogenesis. Proceedings of an International Symposium held in Jerusalem, 21-25 Oct. 1968*. Israel Academy of Sciences and Humanities: Jerusalem, 1969.
28. Pataki, J.; Huggins, C. Molecular Site of Substituents of Benz(a)anthracene Related to Carcinogenicity. *Cancer Research* **1969**, 29, 506-509.
29. Sung, S.-S. Essai d'application de la théorie des régions K et L à un nouveau lot d'hydrocarbures aromatiques polycycliques. *Comptes Rendus de l'Académie des Sciences (Paris)* **1971**, D273, 1247-1250.
30. Sung, S.-S. Essai d'application de la théorie des régions K et L à un nouveau lot d'hydrocarbures aromatiques polycycliques. Etude avec les indices complexes de réactivité. *Comptes Rendus de l'Académie des Sciences (Paris)* **1972**, D274, 1597-1599.
31. Goh, S.H.; Harvey, R.G. K-Region arene oxides of carcinogenic aromatic hydrocarbons. *Journal of the American Chemical Society* **1973**, 95, 242-243.
32. Swaisland, A.J.; Grover, P.L.; Sims, P. Some properties of "K-region" epoxides of polycyclic aromatic hydrocarbons. *Biochemical Pharmacology* **1973**, 22, 1547-1556.
33. Herndon, W.C. Quantum theory of aromatic hydrocarbon carcinogenesis. *International Journal of Quantum Chemistry* **1974**, 8, 123-134.
34. Jones, D.W.; Matthews, R.S. Carcinogenicity and Structure in Polycyclic Hydrocarbons. In *Progress in Medicinal Chemistry*, Ellis, G. P.; West, G. B., Eds. Elsevier: 1974; Vol. Volume 10, pp 159-203.
35. Berger, G.D.; Smith, I.A.; Seybold, P.G.; Serve, M.P. Correlation of an electronic reactivity index with carcinogenicity in polycyclic aromatic hydrocarbons. *Tetrahedron Letters* **1978**, 19, 231-234.
36. Jerina, D.M.; Yagi, H.; Lehr, R.E.; Thakker, D.R.; Schaefer-Ridder, M.; Karle, J.M.; Levin, W., et al. The Bay-Region Theory of Carcinogenesis by Polycyclic Aromatic Hydrocarbons In *Polycyclic Aromatic Hydrocarbons and Cancer. Vol. 1. Environment, Chemistry, and Metabolism*, Gelboin, H. V., Ed. Academic Press: New York, 1978; pp 173-188.
37. Smith, I.A.; Berger, G.D.; Seybold, P.G.; Servé, M.P. Relationships between Carcinogenicity and Theoretical Reactivity Indices in Polycyclic Aromatic Hydrocarbons. *Cancer Research* **1978**, 38, 2968-2977.
38. Miyashita, Y.; Seki, T.; Takahashi, Y.; Daiba, S.-I.; Tanaka, Y.; Yotsui, Y.; Abe, H., et al. Computer-assisted structure—carcinogenicity studies on polycyclic aromatic hydrocarbons by pattern recognition methods. *Analytica Chimica Acta* **1981**, 133, 603-613.
39. Lall, R.S. Structure-Activity Relationship in Hydrocarbon Carcinogens. *MATCH. Commun. Math. Comput. Chem.* **1984**, 15, 251-261.
40. Von Szentpaly, L. Carcinogenesis by polycyclic aromatic hydrocarbons: a multilinear regression on new type PMO indexes. *Journal of the American Chemical Society* **1984**, 106, 6021-6028.
41. Frierson, M.R.; Klopman, G.; Rosenkranz, H.S. Structure-activity relationships (SARs) among mutagens and carcinogens: A review. *Environmental Mutagenesis* **1986**, 8, 283-327.



42. Sakamoto, Y.; Watanabe, S. On the Relationship Between the Chemical Structure and the Carcinogenicity of Polycyclic and Chlorinated Monocyclic Aromatic Compounds as Studied by Means of ^{13}C NMR. *Bulletin of the Chemical Society of Japan* **1986**, 59, 3033-3038.
43. Gayoso, J.; Kimri, S. Sur une tentative d'unification des théories quantiques de la cancérisation par les polyacènes: I. Théorie des régions M, L, et B. *International Journal of Quantum Chemistry* **1990**, 38, 461-486.
44. Barone, P.M.V.B.; Camilo, J.A.; Galvão, D.S. Theoretical Approach to Identify Carcinogenic Activity of Polycyclic Aromatic Hydrocarbons. *Physical Review Letters* **1996**, 77, 1186-1189.
45. Szentpály, L.v.; Ghosh, R. Polycyclic aromatic hydrocarbon carcinogenicity: Theoretical modelling and experimental facts. In *Theoretical and Computational Chemistry*, Cyril, P., Ed. Elsevier: 1998; Vol. 5, pp 447-500.
46. Aihara, J.-i. Reduced HOMO–LUMO Gap as an Index of Kinetic Stability for Polycyclic Aromatic Hydrocarbons. *The Journal of Physical Chemistry A* **1999**, 103, 7487-7495.
47. Vendrame, R.; Braga, R.S.; Takahata, Y.; Galvão, D.S. Structure–Activity Relationship Studies of Carcinogenic Activity of Polycyclic Aromatic Hydrocarbons Using Calculated Molecular Descriptors with Principal Component Analysis and Neural Network Methods. *Journal of Chemical Information and Computer Sciences* **1999**, 39, 1094-1104.
48. Ferreira, M.M.C. Polycyclic aromatic hydrocarbons: a QSPR study. *Chemosphere* **2001**, 44, 125-146.
49. Coluci, V.R.; Vendrame, R.; Braga, R.S.; Galvão, D.S. Identifying Relevant Molecular Descriptors Related to Carcinogenic Activity of Polycyclic Aromatic Hydrocarbons (PAHs) Using Pattern Recognition Methods. *Journal of Chemical Information and Computer Sciences* **2002**, 42, 1479-1489.
50. Flesher, J.W.; Horn, J.; Lehner, A.F. The Meso-Region Theory of Aromatic Hydrocarbon Carcinogenesis. *Polycyclic Aromatic Compounds* **2002**, 22, 379-393.
51. Ruiz-Morales, Y. HOMO–LUMO Gap as an Index of Molecular Size and Structure for Polycyclic Aromatic Hydrocarbons (PAHs) and Asphaltenes: A Theoretical Study. I. *The Journal of Physical Chemistry A* **2002**, 106, 11283-11308.
52. Fias, S.; Fowler, P.W.; Delgado, J.L.; Hahn, U.; Bultinck, P. Correlation of Delocalization Indices and Current-Density Maps in Polycyclic Aromatic Hydrocarbons. *Chemistry – A European Journal* **2008**, 14, 3093-3099.
53. Vijayalakshmi, K.P.; Suresh, C.H. Theoretical studies on the carcinogenicity of polycyclic aromatic hydrocarbons. *Journal of Computational Chemistry* **2008**, 29, 1808-1817.
54. Gómez-Jeria, J.S. 45 Years of the KPG Method: A Tribute to Federico Peradejordi. *Journal of Computational Methods in Molecular Design* **2017**, 7, 17-37.
55. Gómez-Jeria, J.S.; Latorre-Castro, P. On the relationship between electronic structure and carcinogenic activity in substituted Benz[a]anthracene derivatives. *Der Pharma Chemica* **2016**, 8, 84-92.
56. Fukui, K.; Fujimoto, H. *Frontier orbitals and reaction paths: selected papers of Kenichi Fukui*. World Scientific: Singapore; River Edge, N.J., 1997.
57. Gómez-Jeria, J.S. Tables of proposed values for the Orientational Parameter of the Substituent. II. *Research Journal of Pharmaceutical, Biological and Chemical Sciences* **2016**, 7, 2258-2260.
58. Gómez-Jeria, J.S. Tables of proposed values for the Orientational Parameter of the Substituent. I. Monoatomic, Diatomic, Triatomic, $n\text{-C}_n\text{H}_{2n+1}$, $\text{O-}n\text{-C}_n\text{H}_{2n+1}$, NRR' , and Cycloalkanes (with a single ring) substituents. *Research Journal of Pharmaceutical, Biological and Chemical Sciences* **2016**, 7, 288-294.
59. Gómez-Jeria, J.S. *STERIC: A program for calculating the Orientational Parameters of the substituents 2.0*; Santiago, Chile, 2015.
60. Gómez-Jeria, J.S. A New Set of Local Reactivity Indices within the Hartree-Fock-Roothaan and Density Functional Theory Frameworks. *Canadian Chemical Transactions* **2013**, 1, 25-55.



61. Gómez-Jeria, J.S. *Elements of Molecular Electronic Pharmacology (in Spanish)*. 1st ed.; Ediciones Sokar: Santiago de Chile, 2013.
62. Gómez-Jeria, J.S.; Ojeda-Vergara, M. Parametrization of the orientational effects in the drug-receptor interaction. *Journal of the Chilean Chemical Society* **2003**, 48, 119-124.
63. Gómez-Jeria, J.S. Modeling the Drug-Receptor Interaction in Quantum Pharmacology. In *Molecules in Physics, Chemistry, and Biology*, Maruani, J., Ed. Springer Netherlands: 1989; Vol. 4, pp 215-231.
64. Gómez-Jeria, J.S. On some problems in quantum pharmacology I. The partition functions. *International Journal of Quantum Chemistry* **1983**, 23, 1969-1972.
65. Gómez-Jeria, J.S.; Surco-Luque, J.C. A Quantum Chemical Analysis of the Relationships between Electronic Structure and the inhibition of Botulinum Neurotoxin serotype A by a series of Derivatives possessing an 8-hydroxyquinoline core. *Chemistry Research Journal* **2017**, 2, 1-11.
66. Gómez-Jeria, J.S.; Moreno-Rojas, C. Dissecting the drug-receptor interaction with the Klopman-Peradejordi-Gómez (KPG) method. I. The interaction of 2,5-dimethoxyphenethylamines and their N-2-methoxybenzyl-substituted analogs with 5-HT1A serotonin receptors. *Chemistry Research Journal* **2017**, 2, 27-41.
67. Gómez-Jeria, J.S.; Castro-Latorre, P.; Kpotin, G. Quantum Chemical Study of the Relationships between Electronic Structure and Antiviral Activities against Influenza A H1N1, Enterovirus 71 and Coxsackie B3 viruses of some Pyrazine-1,3-thiazine Hybrid Analogues. *International Journal of Research in Applied, Natural and Social Sciences* **2017**, 5, 49-64.
68. Gómez-Jeria, J.S.; Becerra-Ruiz, M.B. Electronic structure and rat fundus serotonin receptor binding affinity of phenethylamines and indolealkylamines. *International Journal of Advances in Pharmacy, Biology and Chemistry* **2017**, 6, 72-86.
69. Robles-Navarro, A.; Gómez-Jeria, J.S. A Quantum-Chemical Analysis of the Relationships between Electronic Structure and Citotoxicity, GyrB inhibition, DNA Supercoiling inhibition and anti-tubercular activity of a series of quinoline-aminopiperidine hybrid analogues. *Der Pharma Chemica* **2016**, 8, 417-440.
70. Kpotin, G.A.; Atohoun, G.S.; Kuevi, U.A.; Houngue-Kpota, A.; Mensah, J.-B.; Gómez-Jeria, J.S. A quantum-chemical study of the relationships between electronic structure and anti-HIV-1 activity of a series of HEPT derivatives. *Journal of Chemical and Pharmaceutical Research* **2016**, 8, 1019-1026.
71. Kpotin, G.; Atohoun, S.Y.G.; Kuevi, U.A.; Kpota-Houngue, A.; Mensah, J.-B.; Gómez-Jeria, J.S. A Quantum-Chemical study of the Relationships between Electronic Structure and Trypanocidal Activity against Trypanosoma Brucei Brucei of a series of Thiosemicarbazone derivatives. *Der Pharmacia Lettre* **2016**, 8, 215-222.
72. Gómez-Jeria, J.S.; Salazar, R. A DFT study of the inhibition of FMS-like tyrosine kinase 3 and the antiproliferative activity against MV4-11 cells by N-(5-(tert-butyl)isoxazol-3-yl)-N'-phenylurea analogs. *Der Pharma Chemica* **2016**, 8, 1-9.
73. Gómez-Jeria, J.S.; Orellana, Í. A theoretical analysis of the inhibition of the VEGFR-2 vascular endothelial growth factor and the anti-proliferative activity against the HepG2 hepatocellular carcinoma cell line by a series of 1-(4-((2-oxoindolin-3-ylidene)amino)phenyl)-3-arylureas. *Der Pharma Chemica* **2016**, 8, 476-487.
74. Gómez-Jeria, J.S.; Moreno-Rojas, C. A theoretical study of the inhibition of human 4-hydroxyphenylpyruvate dioxygenase by a series of pyrazalone-quinazolone hybrids. *Der Pharma Chemica* **2016**, 8, 475-482.
75. Gómez-Jeria, J.S.; Matus-Perez, M. A quantum chemical analysis of the inhibition of protein kinase A (PKA) and Rho-associated protein kinase-2 (ROCK2) by a series of urea-based molecules. *Der Pharma Chemica* **2016**, 8, 1-11.
76. Gómez-Jeria, J.S.; Kpotin, G.A. A note on the inhibition of steroid 11 β -hydroxylase, aldosterone synthase and aromatase by a series of coumarin derivatives *Der Pharma Chemica* **2016**, 8, 213-226.



77. Gómez-Jeria, J.S.; Gazzano, V. A quantum chemical study of the inhibition of α -glucosidase by a group of oxadiazole benzohydrazone derivatives. *Der Pharma Chemica* **2016**, 8, 21-27.
78. Gómez-Jeria, J.S.; Cornejo-Martínez, R. A DFT study of the inhibition of human phosphodiesterases PDE3A and PDE3B by a group of 2-(4-(1H-tetrazol-5-yl)-1H-pyrazol-1-yl)-4-(4-phenyl)thiazole derivatives. *Der Pharma Chemica* **2016**, 8, 329-337.
79. Gómez-Jeria, J.S.; Castro-Latorre, P.; Kpotin, G. Quantum Chemical Analysis of the Relationships between Electronic Structure and Antiviral Activity against HIV-1 of some Pyrazine-1,3-thiazine Hybrid Analogues. *Der Pharma Chemica* **2016**, 8, 234-239.
80. Gómez-Jeria, J.S.; Bravo, H.R. A preliminary DFT analysis of phenolic acids in connection with their phytotoxic activity. *Der Pharma Chemica* **2016**, 8, 25-34.
81. Gómez-Jeria, J.S.; Abarca-Martínez, S. A theoretical analysis of the cytotoxicity of a series of β -carboline-dithiocarbamate derivatives against prostatic cancer (DU-145), breast cancer (MCF-7), human lung adenocarcinoma (A549) and cervical cancer (HeLa) cell lines. *Der Pharma Chemica* **2016**, 8, 507-526.
82. Gómez-Jeria, J.S.; Ojeda-Vergara, M. Electrostatic medium effects and formal quantum structure-activity relationships in apomorphines interacting with D1 and D2 dopamine receptors. *International Journal of Quantum Chemistry* **1997**, 61, 997-1002.
83. Gómez-Jeria, J.S.; Cassels, B.K.; Saavedra-Aguilar, J.C. A quantum-chemical and experimental study of the hallucinogen (\pm)-1-(2,5-dimethoxy-4-nitrophenyl)-2-aminopropane (DON). *European Journal of Medicinal Chemistry* **1987**, 22, 433-437.
84. Frisch, M.J.; Trucks, G.W.; Schlegel, H.B.; Scuseria, G.E.; Robb, M.A.; Cheeseman, J.R.; Montgomery, J., J.A., et al. *G03 Rev. E.01*, Gaussian: Pittsburgh, PA, USA, 2007.
85. Statsoft. *Statistica v. 8.0*, 2300 East 14 th St. Tulsa, OK 74104, USA, 1984-2007.
86. Badger, G.M. The Carcinogenic Hydrocarbons: Chemical Constitution and Carcinogenic Activity. *British Journal of Cancer* **1948**, 2, 309-350.
87. Badger, G.M.; Cook, J.W.; Hewett, C.L.; Kennaway, E.L.; Kennaway, N.M.; Martin, R.H. The Production of Cancer by Pure Hydrocarbons. VI. *Proceedings of the Royal Society of London. Series B - Biological Sciences* **1942**, 131, 170-182.
88. Badger, G.M.; Cook, J.W.; Hewett, C.L.; Kennaway, E.L.; Kennaway, N.M.; Martin, R.H.; Robinson, A.M. The Production of Cancer by Pure Hydrocarbons. V. *Proceedings of the Royal Society of London. Series B - Biological Sciences* **1940**, 129, 439-467.

